

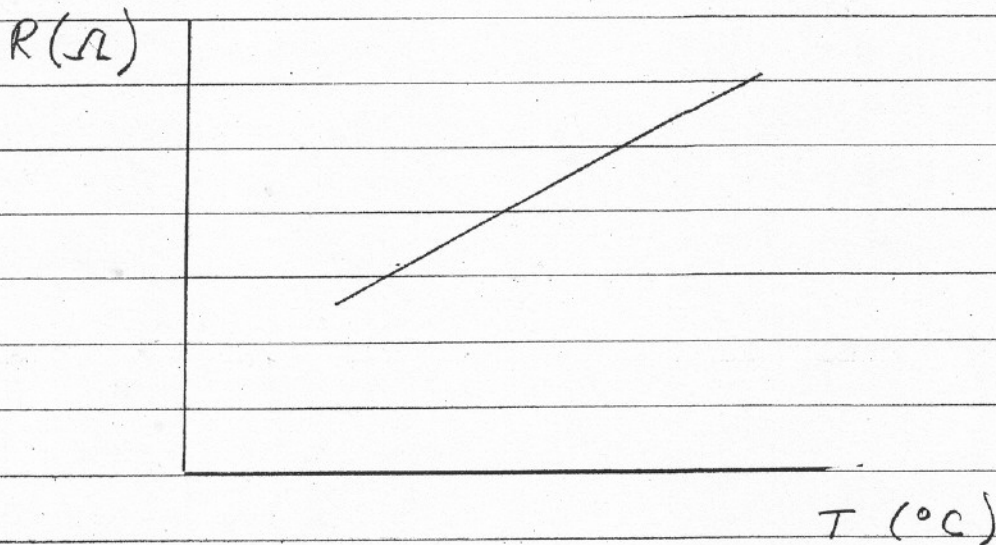
RTD - Resistance Temperature Detector

Thermistor - Thermal Resistor

The electrical resistance of these sensors varies with temperature

$$R = R(T)$$

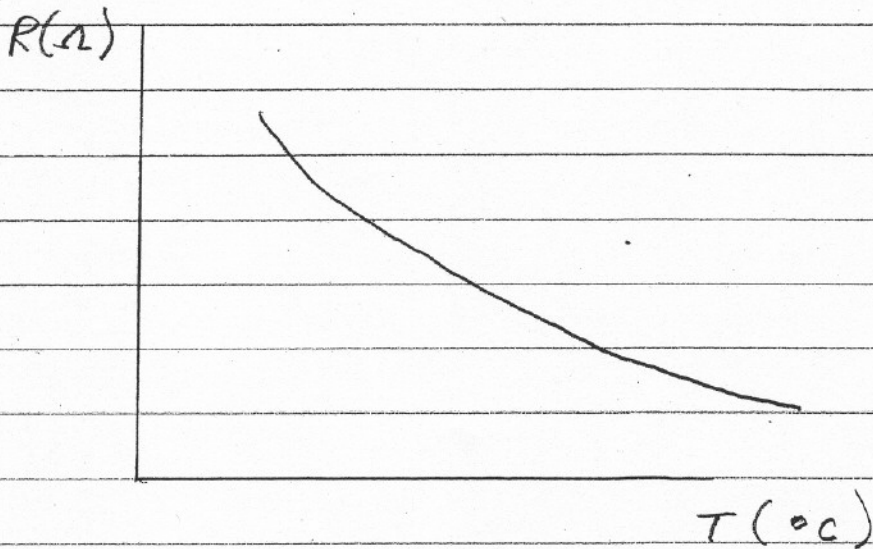
RTD - constructed from metal wire



R increases with increasing T

function $R(T)$ is linear

Thermistors - constructed from temperature sensitive ceramic semiconductors



R decreases with increasing T

function $R(T)$ is non/linear

RTD

coiled wire used to eliminate mechanical strain; mechanical strain changes the resistance of the wire \Rightarrow strain gage

Linear Model

$$R(T) = R_0 [1 + \alpha(T - T_0)]$$

$$\frac{R}{R_0} = 1 + \alpha(T - T_0) \quad (1)$$

T_0 - reference temperature ($^{\circ}\text{C}$)

R_0 - reference resistance (Ω)

α - thermal coefficient of resistivity ($1/^{\circ}\text{C}$)

Use

Need to measure electrical resistance
and then determine T from a calibration
plot or equation (1)

Accuracy

Uncertainty in temperature measurement
 $\pm 0.005^{\circ}\text{C}$; probably 1 σ bound.

RTD Resistance Measurement

1. Conventional ohm meters

small current flow through RTD causes I^2R heating of RTD; called loading error

2. Wheatstone bridge

no current through RTD; no loading error

accurate resistance measurement

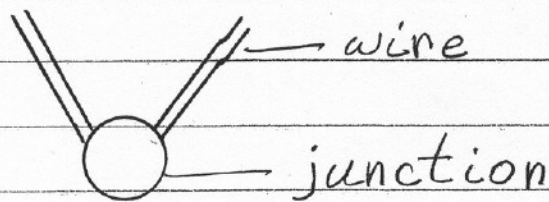
resistance of leads connecting RTD can

cause large errors

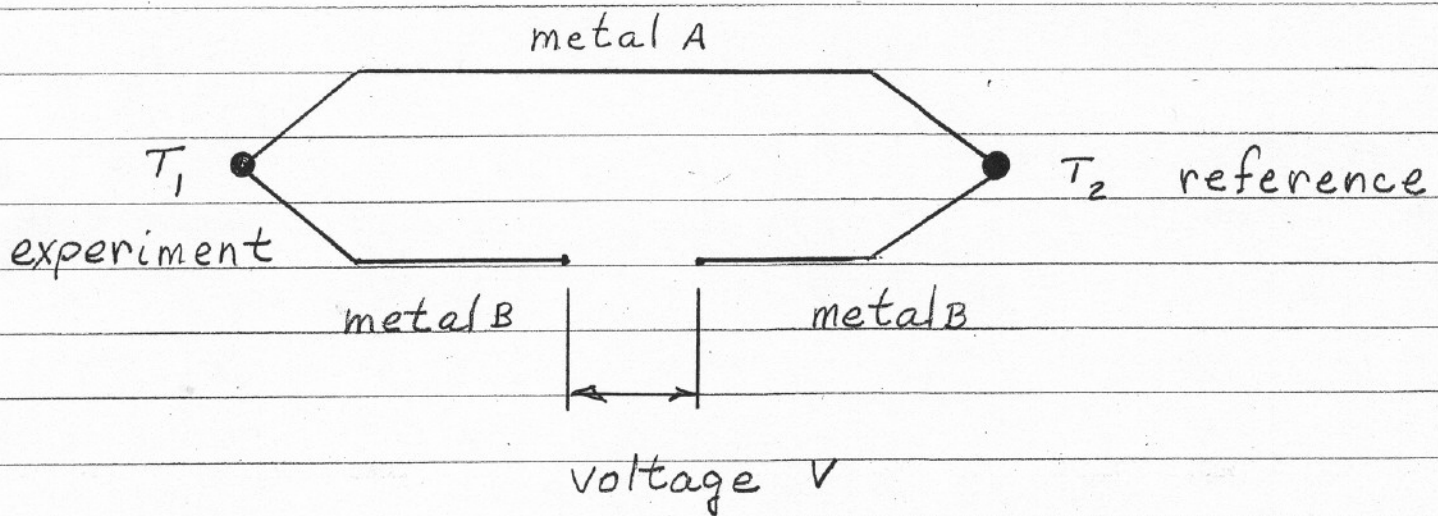
How can you measure time varying temperatures with an RTD?

Thermocouple

consists of two electrical conductors made of different metals with one end of each welded together.



Thermocouple Circuit



$T_1 \neq T_2 \Rightarrow$ open-circuit voltage V

$$V = V(T_1 - T_2; A \text{ \& } B)$$

Thermoelectric Phenomena result from the simultaneous flow of heat and electrical

current in the an electrical conductor

Theoretical basis involves irreversible
thermodynamics

THERMOCOUPLES

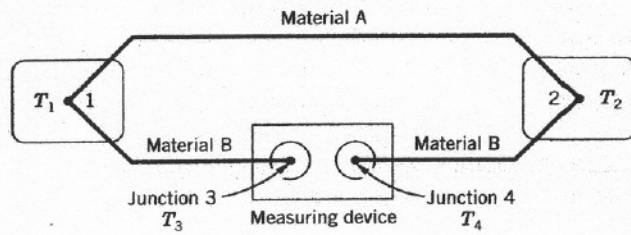


Figure 8.14 Typical thermocouple measuring circuit.

Seebeck Effect

A potential difference, or emf, is produced in an open thermocouple circuit when a temperature difference is applied across the junctions.

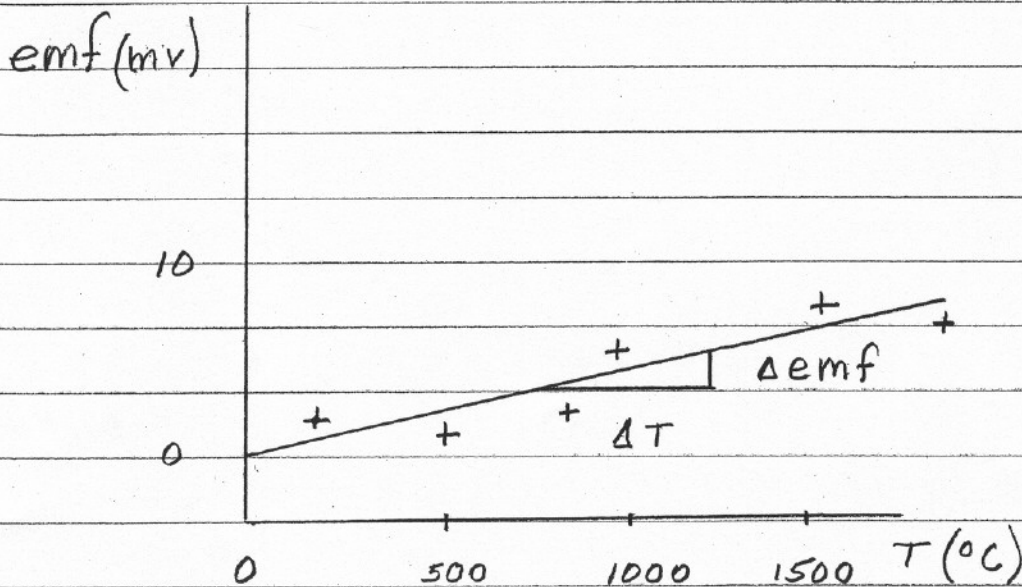
open circuit means no current flow

There is a fixed functional relationship between the emf and the temperatures T_1 and T_2 . See Figure 8.13.

static Calibration generates the curve

Seebeck Coefficient

$$\alpha_{AB} = \frac{d(\text{emf})}{dT} \Big|_{\text{open circuit}} = \frac{\Delta \text{emf}}{\Delta T}$$



We need to measure the emf, voltage, across the terminals labeled junction 3 and junction with minimal current flowing through the circuit. Use a high impedance voltmeter.

A current will introduce other thermoelectric effects that change the calibration.

Dynamic Calibration

Use the 1st-order linear model discussed
in the last lecture

$$\tau \frac{dT}{dt} + T = cU(t)$$

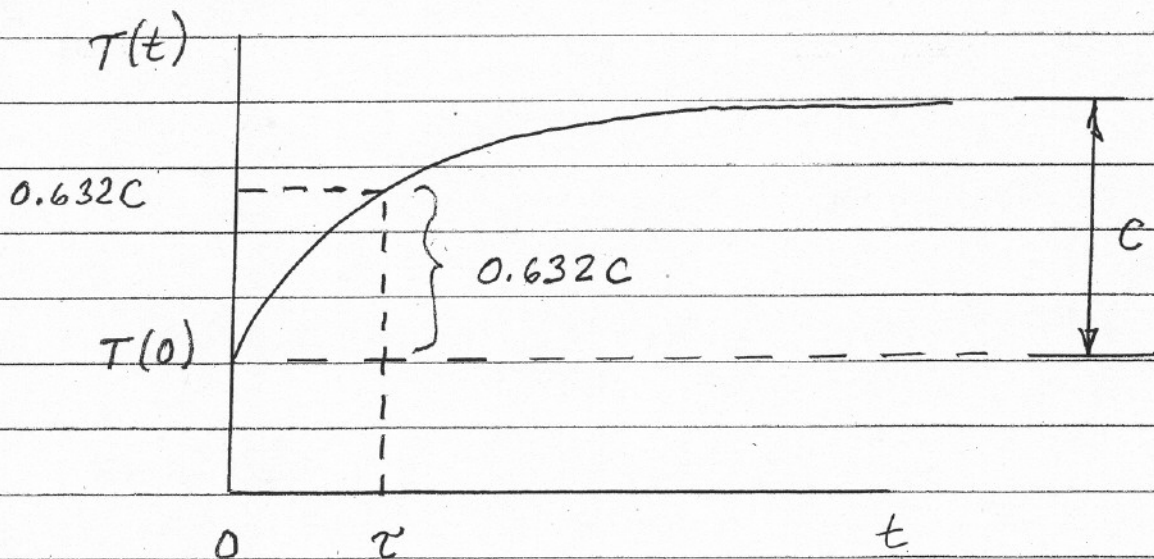
solution

$$T(t) = T(0) + c(1 - e^{-t/\tau})$$

$T(0)$ - initial temperature

c - change in ambient temperature

τ - time constant



Suppose $t = \tau$

$$\frac{T(t) - T(0)}{C} = 1 - e^{-1} = 0.632$$

Fundamental Thermocouple Laws

1. Law of Homogeneous Materials

You need two different metal wires to make a thermocouple.

2. Law of Intermediate Materials

If two junctions of a thermocouple circuit are at the same temperature, the resultant emf will not change from the open circuit emf

3. Law of Intermediate Temperatures

$$\text{If } T_1 \neq T_2 \Rightarrow \text{emf}_1$$

$$T_2 \neq T_3 \Rightarrow \text{emf}_2$$

$$\text{Then } T_1 \neq T_3 \Rightarrow \text{emf}_1 + \text{emf}_2$$

314 Chapter 8 Temperature Measurements

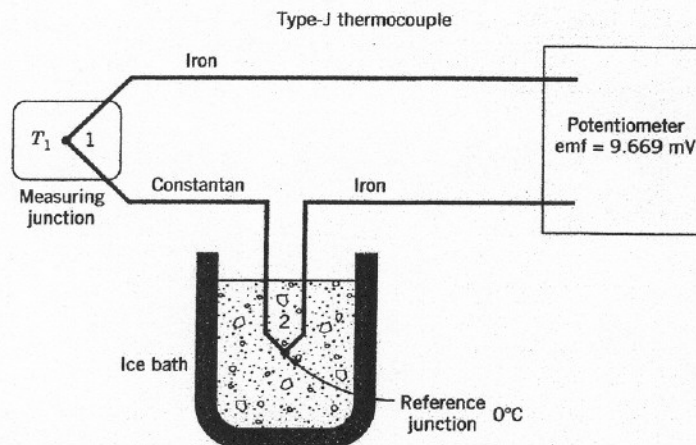


Figure 8.19 Thermocouple circuit for Example 8.6.

an ice-point bath. The voltage output is measured with a potentiometer and is found to be 9.669 mV . What is T_1 ?

KNOWN

A thermocouple circuit having one junction at 0°C and a second junction at an unknown temperature. The circuit produces an emf of 9.669 mV .

FIND

The temperature T_1 .

ASSUMPTION

Thermocouple follows NIST standard.

SOLUTION

Standard thermocouple tables such as Table 8.6 are referenced to 0°C . The temperature of the reference junction for this case is 0°C . Therefore, the temperature corresponding to an output voltage may simply be determined from Table 8.6, in this case as 180°C .

COMMENT

Because of the law of intermediate metals, the junctions formed at the potentiometer do not affect the voltage measured for the thermocouple circuit, and the voltage output reflects accurately the temperature difference between junctions 1 and 2.

EXAMPLE 8.7

Suppose the thermocouple circuit in the previous example (Example 8.6) now has junction 2 maintained at a temperature of 30°C and produces an output voltage of 8.132 mV . What temperature is sensed by the measuring junction?

KNOWN

T_2 is 30°C, and the output emf is 8.132 mV.

ASSUMPTION

Thermocouple follows NIST standard.

FIND

The temperature of the measuring junction.

SOLUTION

By the law of intermediate temperatures the output emf for a thermocouple circuit having two junctions, one at 0°C and the other at T_1 , would be the sum of the emfs for a thermocouple circuit between 0 and 30°C and between 30°C and T_1 . Thus,

$$\text{emf}_{0-30} + \text{emf}_{30-T_1} = \text{emf}_{0-T_1}$$

This relationship allows the voltage reading from the nonstandard reference temperature to be converted to a 0°C reference temperature by adding $\text{emf}_{0-30} = 1.537$ to the existing reading. This results in an equivalent output voltage, referenced to 0°C as

$$1.537 + 8.132 = 9.669 \text{ mV}$$

Clearly, this thermocouple is sensing the same temperature as in the previous example, 180°C. This value is determined from Table 8.6.

COMMENT

Note that the effect of raising the reference junction temperature is to lower the output voltage of the thermocouple circuit. Negative values of voltage, as compared with the polarity listed in Table 8.4, indicate that the measured temperature is less than the reference junction temperature.